



Dez 5-10:09

$\exists j, a, b, c, m:$

 $\text{name}(j, \text{"John"}) \wedge \dots \wedge \text{married}(j, m)$

 $\wedge \text{Child}(j, a) \wedge \text{child}(j, b) \wedge \text{child}(j, c)$

 $\wedge \text{name}(a, \text{"Alice"}) \wedge \dots$

 $\wedge \text{name}(b, \text{"Bob"}) \wedge \dots$

 $\wedge \text{age}(c, 12)$

 $\wedge \text{name}(m, \text{"Mary"}) \wedge \text{child}(m, a) \wedge \text{child}(m, b) \wedge \text{child}(m, c)$

Dez 5-10:34

recall: 2-variables fragment of FOL is decidable

$\exists x$: name(x, "John") $\wedge \exists y$ (married(x,y) **2Vars: x, y**)

$\exists y$: (~~child~~ child(x,y) \wedge name(y, 'Alice') \wedge age(y, 10)

$\wedge \exists x$ (hasDog(y,x) \wedge Dog(x) \wedge name(x, 'Odie') \wedge ...)

$\wedge \exists y$ (child(x,y) \wedge name(y, 'Bob') \wedge age(y, 8))

$\wedge \exists y$ (child(x,y) \wedge age(y, 12))

\Rightarrow TREES can be expressed using only 2 variables

Graph (john, maris, alice, bob) CANNOT be expressed by 2Vars.

"Tree property"

Dez 5-10:39

SE172 $\psi \rightarrow \varphi$, ψ consistent

$\hat{=}$ Query $\varphi(x)$?

\rightarrow Tableau

ψ

$\neg \varphi(x)$

$\psi \rightarrow \varphi$, ψ inconsistent \Rightarrow error

$\neg \varphi(x)$ not needed for closing

$\square \square$ for ψ alone \rightarrow query is a yes answer

Quantifiers for X when tableau closes

Dez 5-10:51