# Chapter 7 Ontologies and the Web Ontology Language – OWL

- vocabularies can be defined by RDFS
  - not so much stronger than the ER Model or UML (even weaker: no cardinalities)
  - not only a conceptual model, but a "real language" with a close connection to the data level (RDF)
  - incremental world-wide approach
  - "global" vocabulary can be defined by autonomous partners
- but: still restricted when describing the vocabulary.

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Ontologies/ontology languages further extend the expressiveness:

- Description Logics
- Topic Maps (in SGML) since early 90s, XTM (XML Topic Maps)
- Ontolingua non-XML approach from the Knowledge Representation area
- OIL (Ontology Inference Layer): initiative funded by the EU programme for Information Society Technologies (project: On-To-Knowledge, 1.2000-10.2002); based on RDF/RDFS
- DAML (Darpa Agent Markup Language; 2000) ... first ideas for a Semantic Web language
- DAML+OIL (Jan. 2001)
- developed into OWL (1st version March 02, finalized Feb. 04)

# THREE VARIANTS OF OWL

Several expressiveness/complexity/decidability levels:

- OWL Full: extension of RDF
  - classes can also be regarded as individuals (classes of classes ... higher-order reasoning)
- OWL DL
  - fragment of OWL that fits into the Description Logics Framework
  - decidable reasoning
  - OWL 1.0: Feb. 2004, OWL 1.1/2.0 work in progress
- OWL Lite
  - subset of OWL DL
  - easier migration from frame-based tools
     (note: F-Logic was a frame-based framework)
  - easier reasoning

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# 7.1 Description Logics

- Focus on the description of concepts, not of instances
- Terminological Reasoning
- Origin of DLs: Semantic Networks (graphical formalism)

### **Notions**

- Concepts (= classes),
   note: literal datatypes (string, integer etc.) are not classes in DL and OWL, but data ranges
  - (cf. XML Schema: distinction between simpleTypes and complexTypes)
- Roles (= relationships),
- A Description Logic alphabet consists of a finite set of concept names (e.g. Person, Cat, LivingBeing, Male, Female, ...) and a finite set of role names (e.g., hasChild, marriedTo, ...),
- constructors for derived concepts and roles,
- axioms for asserting facts about concepts and roles.

# **COMPARISON WITH OTHER LOGICS**

Syntax and semantics defined different but similar from first-order logic

- formulas over an alphabet and a small set of additional symbols and combinators
- semantics defined via interpretations of the combinators
- set-oriented, no instance variables
   (FOL: instance-oriented with domain quantifiers)
- family of languages depending on what combinators are allowed.

The base: AL

The usual starting point is AL:

- "attributive language"
- Manfred Schmidt-Schauss and Gert Smolka: Attributive Concept Descriptions with Complements. In Artificial Intelligence 48(1), 1991, pp. 1–26.
- extensions (see later: ALC, ALCQ, ALCQ(D), ALCQI, ALCN etc.)

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# ATOMIC, NAMED CONCEPTS

- atomic concepts, e.g., Person, Male, Female
- the "universal concept" ⊤ (often called "Thing" everything is an instance of Thing)
- the empty concept  $\perp$  ("Nothing"). There is no thing that is an instance of  $\perp$ .

# **SET OPERATIONS**

- intersection of concepts:  $A \sqcap B$
- negation: ¬A
   AL allows only atomic negation.
- union:  $A \sqcup B$ Union is not allowed in  $\mathcal{AL}$ .

### INTENSIONAL CONCEPTS

Concepts (as an intensional characterization of sets of instances) can be described implicitly by their properties (wrt. *roles*).

Let R be a role, C a concept. Then, the expressions  $\exists R.C$  and  $\forall R.C$  also describe concepts (intensionally defined concepts) by constraining the roles:

- Existential quantification:  $\exists R.C$  all things that have a *filler* for the role R that is in C.  $\exists$ hasChild.Male describes all things that have a male child.
- $\mathcal{AL}$ : only as restricted existential quantification:  $\exists R. \top \exists \mathsf{hasChild}. \top \mathsf{describes}$  all things that have a child (formally: that belongs to the concept "Thing").
- Range constraints:  $\forall R.C$   $\forall$ hasChild.Male describes all things that have only male children (including those that have no children at all).
- Note that  $\bot$  can be used to express non-existence:  $\forall R.\bot$  describes all things where all fillers of role R are of the concept  $\bot$  (= Nothing) i.e., all things that do not have a filler for the role R.

∀hasChild. ⊥ describes the things that have no children.

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# SEMANTICS OF CONCEPT CONSTRUCTORS

As usual: by interpretations.

An interpretation  $\mathcal{I}$  consists of the following:

- a domain  $\mathcal{D}$ ,
- for every concept name  $C: C^{\mathcal{I}} \subseteq \mathcal{D}$  is a subset of the domain,
- for every role name  $R: R^{\mathcal{I}} \subseteq \mathcal{D} \times \mathcal{D}$  is a binary relation over the domain.

### Structural Induction

- $(A \sqcup B)^{\mathcal{I}} = A^{\mathcal{I}} \cup B^{\mathcal{I}}$
- $\bullet \ (A \sqcap B)^{\mathcal{I}} = A^{\mathcal{I}} \cap B^{\mathcal{I}}$
- $\bullet \ (\neg A)^{\mathcal{I}} = \mathcal{D} \setminus A^{\mathcal{I}}$
- $(\exists R.C)^{\mathcal{I}} = \{x \mid \text{ there is an } y \text{ such that } (x,y) \in R^{\mathcal{I}} \text{ and } y \in C^{\mathcal{I}}\}$
- $\bullet \ \, (\forall R.C)^{\mathcal{I}} = \{x \ \mid \ \, \text{for all} \,\, y \,\, \text{such that} \,\, (x,y) \in R^{\mathcal{I}}, \, y \in C^{\mathcal{I}}\}$

### Example

Male  $\sqcap \forall$  has Child. Male is the set of all men who have only sons.

# STRUCTURE OF A DL KNOWLEDGE BASE

# **DL Knowledge Base**

# TBox (schema)

Talks about concepts

 $Man \equiv Human \sqcap Male$ 

Parent  $\equiv$  Human  $\sqcap$  ( $\exists > 1$  hasChild. $\top$ )

ParentOfSons  $\equiv$  Human  $\sqcap$  ( $\exists \ge 1$  hasChild.Male)

ParentOfOnlySons  $\equiv$  Human  $\sqcap$  ( $\forall$  hasChild.Male)

# ABox (data)

Talks about individuals

Person(John), Male(John)

hasChild(John,Alice), age(Alice,10), Female(Alice)

hasChild(John,Bob), age(Bob,8), Male(Bob)

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# THE TBOX: TERMINOLOGICAL AXIOMS

Definitions and assertions (not to be understood as constraints) about concepts:

- concept subsumption:  $C \sqsubseteq D$ ; defining a concept hierarchy.  $\mathcal{I} \models C \sqsubseteq D : \Leftrightarrow C^{\mathcal{I}} \subseteq D^{\mathcal{I}}$ .
- concept equivalence:  $C \equiv D$ ; often used for defining the left-hand side concept. Semantics:  $\mathcal{I} \models C \equiv D :\Leftrightarrow C \sqsubseteq D$  and  $D \sqsubseteq C$ .
- analogous for role subsumption and role equivalence.

### **TBox Reasoning**

- is a concept *C* satisfiable?
- is  $C \sqsubseteq D$  implied by a TBox
- given the definition of a new concept *D*, classify it wrt. the given concept hierarchy.

# THE ABOX: ASSERTIONAL AXIOMS

 contains the facts about instances (using names for the instances) in terms of the basic concepts and roles:

Person(John), Male(John), hasChild(John,Alice)

• contains also knowledge in terms of intensional concepts, e.g., ∃hasChild.Male(John)

### TBox + ABox Reasoning

- check consistency between ABox and a given TBox
- ask whether a given instance satisfies a concept C
- ask for all instances that have a given property
- ask for the most specific concepts that an instance satisfies

Note: instances are allowed only in the ABox, not in the TBox.

If instances should be used in the definition of concepts (e.g., "European Country" or "Italian City"), *Nominals* must be used (see later).

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# EXTENSIONS TO $\mathcal{AL}$

- $\mathcal{U}$ : "union"; e.g. Parent  $\equiv$  Father  $\sqcup$  Mother.
- C: negation ("complement") of non-atomic concepts.

Person  $\neg \neg \exists hasChild. \top$  characterizes the set of persons who have no children (note: open-world semantics of negation!)

Note: the FOL equivalent would be expressed via variables:

 $\forall x (\mathsf{Childless}(x) \leftrightarrow (\mathsf{Person}(x) \land \neg \exists y (\mathsf{hasChild}(x,y))))$ 

•  $\mathcal{E}$ : unrestricted existential quantification of the form  $\exists R.C.$   $\exists$ hasChild.Male

Note: the FOL equivalent uses variables:

 $p(x) \leftrightarrow \exists y (\mathsf{hasChild}(x, y) \land \mathsf{male}(y))$ ),

or ∃hasChild.hasChild.⊤ for grandparents.

- $\mathcal{N}$ : (unqualified) cardinalities of roles ("number restrictions"). ( $\geq 3$  hasChild. $\top$ ) for persons who have at least 3 children.
- Q: qualified role restrictions like ( $\leq 2$  hasChild.Male). A weaker form,  $\mathcal{F}$ , is restricted to cardinalites 0, 1 and "arbitrary".

# THE EXTENDED LANGUAGES

•  $\mathcal{AL}$  has no "branching" (no union, or any kind of disjunction; so tableau proofs in  $\mathcal{AL}$  are linear.

Exercise: show why unrestricted existential quantification  $\exists R.C$  in contrast to  $\exists R.\top$  leads to branching.

- The logics are named by the letters, e.g.  $\mathcal{ALUN}$  for  $\mathcal{AL}$  with union and unqualified n-cardinalities.
- *U* and *E* can be expressed by *C*.
   Thus, *ALC* is frequently used.
- ullet  $\mathcal{ALC}$  is the "smallest" Description Logic that is closed wrt. the set operations.
- A frequently used restriction of  $\mathcal{AL}$  is called  $\mathcal{FL}^-$  (for "Frame-Language"), which is obtained by disallowing negation completely (i.e., having only positive knowledge).

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# COMPLEXITY AND DECIDABILITY: OVERVIEW

- Logic  $\mathcal{L}^2$ , i.e., FOL with only two (reusable) variable symbols is decidable.
- Full FOL is undecidable.
- DLs: incremental, modular set of semantical notions.
- only part of FOL is required for concept reasoning.
- ALC can be expressed by FOL, but then, the inherent semantics is lost → full FOL reasoner required.
- Actually,  $\mathcal{ALC}$  can be encoded in FOL by only using two variables  $\to \mathcal{ALC}$  is decidable.
- Consistency checking of ALC-TBoxes and -ABoxes is PSPACE-complete (proof by reduction to *Propositional Dynamic Logic* which is in turn a special case of propositional multimodal logics).

There are algorithms that are efficient in the average case.

•  $\mathcal{ALCN}$  goes beyond  $\mathcal{L}^2$  and PSPACE. Reduction to  $\mathcal{C}^2$  (including "counting" quantifiers) yields decidability, but now in NEXPTIME). There are algorithms for  $\mathcal{ALCN}$  and even  $\mathcal{ALCQ}$  in PSPACE.

# **FURTHER EXTENSIONS**

- Role Constructors, i.e., derived roles as union or intersection (hasChild  $\equiv$  hasSon  $\cup$  hasDaughter), concatenation (hasGrandchild  $\equiv$  hasChild  $\circ$  hasChild), transitive closure (hasDescendant  $\equiv$  hasChild $^+$ ) (indicated by e.g.  $\mathcal{ALC}_{reg}$ ), and inverse (isChildOf  $\equiv$  hasChild $^-$ ) ( $\mathcal{I}$ ).
- Data types (indicated by "(D)"), e.g. integers.
   Adult = Person □ ∃age. ≥ 18.
- Nominals (O) allow to use individuals from the ABox also in the TBox.
   GermanCity ≡ ∀inCountry.Germany

They are used in a class constructor like one-of $\{o_1, \ldots, o_n\}$  (for defining enumeration concepts) or in has-value $\{x\}$  for value constraints of properties.

• Role-Value-Maps:

Equality Role-Value-Map:  $(R_1 = R_2) \equiv \{x \mid R_1(x,y) \leftrightarrow R_2(x,y)\}$ . Containment Role-Value-Map:  $(R_1 \subseteq R_2) \equiv \{x \mid R_1(x,y) \rightarrow R_2(x,y)\}$ . knows  $\subseteq$  likes for people who like all people they know.

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# **SEMANTICS OF EXTENSIONS**

- $\bullet \ (\geq nR.C)^{\mathcal{I}} = \{x \ | \ \#\{y \ | \ (x,y) \in R^{\mathcal{I}} \text{ and } y \in C^{\mathcal{I}}\} \geq n\},$
- $\bullet \ (\leq nR.C)^{\mathcal{I}} = \{x \mid \#\{y \mid (x,y) \in R^{\mathcal{I}} \text{ and } y \in C^{\mathcal{I}}\} \leq n\},$
- $\bullet \ (nR.C)^{\mathcal{I}} = \{x \ | \ \#\{y \ | \ (x,y) \in R^{\mathcal{I}} \text{ and } y \in C^{\mathcal{I}}\} = n\},$
- $(R \circ S)^{\mathcal{I}} = \{(x, z) \mid \exists y : (x, y) \in R^{\mathcal{I}} \text{ and } (y, z) \in S^{\mathcal{I}}\},$
- $(R^-)^{\mathcal{I}} = \{(y, x) \mid (x, y) \in R^{\mathcal{I}}\},\$
- $\bullet \ (R^+)^{\mathcal{I}} = (R^{\mathcal{I}})^+.$
- If Nominals are used,  $\mathcal I$  also assigns an element of  $\mathcal D$  to each nominal symbol x.

$$\{i_1, \dots, i_n\}^{\mathcal{I}} = \{i_1^{\mathcal{I}}, \dots, i_n^{\mathcal{I}}\}, \text{ and } R.y = \{x \mid \{z \mid (x, z) \in R^{\mathcal{I}}\} = \{y\}.$$

# **COMPLEXITY OF EXTENSIONS**

- Role constructors:  $\mathcal{ALC}_{reg}$ , including transitivity, composition and union is EXPTIME-complete; this stays the same when inverse roles and even cardinalities for *atomic* roles are added ( $\mathcal{ALCQI}_{reg}$ ).
  - Recall that inverse and transitive closure are important for ontologies.
- Combining such *composite* roles with cardinalities becomes undecidable (encoding in FOL requires 3 variables).
- Encoding of Role-Value Maps with composite roles in FOL is undecidable (encoding in FOL requires 3 variables; the logic loses the *tree model property*).
- $\mathcal{ALCQI}_{reg}$  with role-value maps restricted to boolean compositions of *basic* roles remains decidable. Decidability is also preserved when role-value-maps are restricted to functional roles.

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### DESCRIPTION LOGIC MODEL THEORY

The definition is the same as in FOL:

- an interpretation is a model of an ABox A if
  - for every atomic concept C and individual x such that  $C(x) \in A$ ,  $x^{\mathcal{I}} \in C^{\mathcal{I}}$ , and
  - for every atomic role R and individuals x,y such that  $R(x,y)\in A$ ,  $(x^{\mathcal{I}},y^{\mathcal{I}})\in R^{\mathcal{I}}$ .
- note: the interpretation of the non-atomic concepts and roles is given as before,
- all axioms  $\phi$  of the TBox are satisfied, i.e.,  $\mathcal{I} \models \phi$ .

Based on this, DL entailment is also defined as before:

• a set  $\Phi$  of formulas entails another formula  $\Psi$  (denoted by  $\Phi \models \psi$ ), if  $\Psi^{\mathcal{I}} =$  true in all models of  $\Phi$ .

# DECIDABILITY, COMPLEXITY, AND ALGORITHMS

Many DLs are decidable, but in high complexity classes.

- decidability is due to the fact that often *local* properties are considered, and the verification proceeds tree-like through the graph without connections between the branches.
- This locality does not hold for cardinalities over composite roles, and for role-value maps
   these lead to undecidability.
- Reasoning algorithms for ALC and many extensions are based on tableau algorithms, some use model checking (finite models), others use tree automata.

# Three types of Algorithms

- restricted (to polynomial languages) and complete
- expressive logics with complete, worst-case EXPTIME algorithms that solve realistic problems in "reasonable" time. (Fact, Racer, Pellet)
- more expressive logics with incomplete reasoning.

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### **EXAMPLE**

- Given facts: Person  $\equiv$  Male  $\sqcup$  Female and Person(unknownPerson).
- Query ?-Male(X) yields an empty answer
- Query ?-Female(X) yields an empty answer
- Query ?-(Male 

  Female)(X) yields unknownPerson as an answer
- for guery answering, all models of the TBox+ABox are considered.
- in some models, the unknownPerson is Male, in the others it is female.
- in all models it is in (Male 

  ⊢ Female).