## 2. Unit: SPARQL Formal Semantics

Exercise 2.1 (SPARQL Formal Semantics) Consider the SPARQL Formal Semantics.

- a) Define a "null-tolerant join" for the relational algebra that acts like the  $\bowtie$  of the SPARQL algebra.
- b) Which SQL construct is similar to the "\" operator in the SPARQL algebra?
- c) In the SPARQL algebra, OPT is expressed via left outer join, which is defined via "\" (while a corresponding MINUS does not exist in the SPARQL syntax). Such a MINUS (cf. part (b) of this exercise) provides a more intuitive idea of negation than "! bound(x)". Give a general pattern how to express ( $P_1$  MINUS  $P_2$ ) in SPARQL 1.0 syntax.
- d) Recall the definition of  $\exists \bowtie$  in the relational algebra (DB lecture) and define SPARQL's  $\exists \bowtie$  in a similar way.

Exercise 2.2 (Outer Join) Recall that SPARQL's OPTIONAL corresponds to a left outer join.

- a) Give a general pattern how to express a *full* outer join (i.e., "outer" to both sides) in the SPARQL algebra (consider as input two mappings R and S and give an expression for  $R \exists \bowtie \square S$ ) and in SPARQL.
- b) Give all cities (name as ?XN) that are the capital of a country (:capital) or that are located at a river (:locatedAt) or both (return the names ?CN of the country and/or the river (?RN)).

**Exercise 2.3 (SPARQL Formal Semantics: OPTIONAL)** Consider the SPARQL Formal Semantics.

Prove or show a counterexample:

The statement (from W3C SPARQL Working Draft 20061004)

If OPT(A, B) is an optional graph pattern, where A and B are graph patterns, then S is a solution of OPT(A,B) if

- S is a pattern solution of A and of B, or
- S is a solution to A, but not to A and B.

describes the same semantics as above.