

**Database Theory**  
**Winter Term 2016/17**  
 Prof. Dr. W. May

## 2. Unit: Datalog

Discussion by 14./21.12.2016

**Exercise 1 (Äquivalenz von Algebra und Datalog)** Show that for every expression of the relational algebra there is an equivalent stratified Datalog program.

### Exercise 2 (Datalog to Algebra)

Consider the translation of Datalog programs with a distinguished answer predicate to the relational algebra.

- Given a rule  $B \leftarrow C_1 \wedge \dots \wedge C_m \wedge \neg D_{m+1} \wedge \dots \wedge \neg D_{m+n}$  where the  $C_i$  and  $D_i$  are of the form  $R_i(a_1, \dots, a_\ell)$ ,  $a_j$  constants or variables. Give an algebra expression that returns the relation defined by it.
- Which additional constructs must also be translated?
- Consider the following program:

```

res(X,Z) :- v(X,_,_Y), q(,_,_Y,Z), ¬r(Z,_)
res(X,Z) :- v(X,_,_Y,Z), ¬r(,_,_), ¬w(X)
v(X,Y,Z) :- p(Z,_,X), q(X,Y,_)
v(X,Y,Z) :- p(X,Y,Z), Y<4.
w(X) :- s(,X), t(X,_)
    
```

where  $p/3, q/3, r/2, s/2, t/2$  are EDB relations,  $v/3, w/1$  are IDB relations (views).

Give the algebra expression that corresponds to the `res` predicate.

### Exercise 3 (Stratified Datalog)

Give an example for the nonmonotonicity of the stratified semantics,

show that for a stratifiable program  $P$  there can be multiple minimal models.

**Exercise 4 (Datalog-Anfragen an Mondial: Schweizer Sprachen)** Give Datalog programs for the following queries against the Mondial database. Compare with the same queries in the algebra and in the relational calculus.

- a) All codes of countries in which some language is spoken that is also spoken in Switzerland.
- b) All codes of countries in which only languages are spoken that are not spoken in Switzerland.
- c) All codes of countries in which only languages are spoken that are also spoken in Switzerland.
- d) All codes of countries in which all languages are spoken that are spoken in Switzerland.

### Exercise 5 (Datalog-Anfragen an Mondial: Landlocked)

- Give a Datalog program that returns the names of all countries that have no coast.
- Give a Datalog program that returns the names of all countries that have no coast and that have no neighbor country that has any coast.

- Give the dependency graph of your program.

**Exercise 6 (Aggregation in Datalog/XSB)** Define the aggregation operators in XSB in a module `aggs.P`.

The syntax of the comparison predicates and of the arithmetic operators is given in Sections 3.10.5 (Inline Predicates) and 4.3 (Operators) of the XSB Manual Part I.

Then use `aggs.P` for answering the following queries in Datalog:

- a) Give for each country the name and the number of neighbors.
- b) Give the name of the country that has the highest number of neighbors (and how many).
- c) Give the average area of all continents (to test `avg`).
- d) Give the average latitude and longitude of all cities.