

generate the ground instances of rules of the program that can be useful

basis: all ground instances. Let them, as they are (for copying)

win(a) :- move(a,b), not win(b).
win(a) :- move(a,f), not win(f).
win(b) :- move(b,c), not win(c).
win(b) :- move(b,g), not win(g).
win(b) :- move(b,k), not win(k).
win(c) :- move(c,d), not win(d).
win(c) :- move(c,l), not win(l).
win(d) :- move(d,e), not win(e).
win(e) :- move(e,a), not win(a).
win(g) :- move(g,h), not win(h).
win(g) :- move(g,i), not win(i).
win(h) :- move(h,m), not win(m).
win(i) :- move(i,j), not win(j).
win(l) :- move(l,d), not win(d).
win(m) :- move(m,h), not win(h).

first round:

~~H_0 = emptyset~~ no, start with H_0 = EDB. => win(X) false for all X

~~win(a) :- move(a,b), not win(b).~~

~~win(a) :- move(a,f), not win(f).~~

~~win(b) :- move(b,c), not win(c).~~

~~win(b) :- move(b,g), not win(g).~~

~~win(b) :- move(b,k), not win(k).~~

~~win(c) :- move(c,d), not win(d).~~

~~win(c) :- move(c,l), not win(l).~~

~~win(d) :- move(d,e), not win(e).~~

~~win(e) :- move(e,a), not win(a).~~

~~win(g) :- move(g,h), not win(h).~~

~~win(g) :- move(g,i), not win(i).~~

~~win(h) :- move(h,m), not win(m).~~

\mathcal{H}

~~win(i) :- move(i,j), not win(j).~~

~~win(l) :- move(l,d), not win(d).~~

~~win(m) :- move(m,h), not win(h).~~

(P = the above + all "move"-facts)

new program P^H

run T_P^H ... \omega ... until it stops.

Here, it will stop after one T_P round:

H₁ = {the moves} U { the instantiated heads of these rules }
= {moves} U {win(a), win(b), win(c), win(d), win(e), win(g),
win(h), win(i), win(l), win(m) }

... consider this result:

$$\begin{aligned} H_1 &= \{\text{the moves}\} \cup \{\dots \text{ the instantiated heads of these rules } \} \\ &= \{\text{moves}\} \cup \{\text{win(a), win(b), win(c), win(d), win(e), win(g),} \\ &\quad \text{win(h), win(i), win(l), win(m)} \} \end{aligned}$$

note: for win(f), win(k), win(n) and win(j) there were no rules, so they have not been derived in H_1

=> we know that f,k,n,jj are definitely lost positions

=> from "nothing" , we got an overestimate of the win nodes and a (safe!) underestimate of the lost nodes

2nd round: H_1 : win: abcdeghilm
(means: not win: fjkn)

again, build the reduct P_{H_1} :

first step:

delete from PH_1 all rules that contain a negative literal $\neg a$ in the body such that $a \in H_1$,

second step:

delete all remaining negative literals in the bodies of the remaining rules.
(because those are true ... fix them intermediately)

~~win(a) :- move(a,b), not win(b).~~
win(a) :- move(a,f), not win(f).
~~win(b) :- move(b,c), not win(c).~~
~~win(b) :- move(b,g), not win(g).~~
win(b) :- move(b,k), not win(k).
~~win(c) :- move(c,d), not win(d).~~
~~win(c) :- move(c,l), not win(l).~~
~~win(d) :- move(d,e), not win(e).~~
win(e) :- move(e,a), not win(a).
~~win(g) :- move(g,h), not win(h).~~
~~win(g) :- move(g,i), not win(i).~~
~~win(h) :- move(h,m), not win(m).~~
win(i) :- move(i,j), not win(j).
~~win(l) :- move(l,d), not win(d).~~
~~win(m) :- move(m,h), not win(h).~~

run $T_{PH_1} \rightarrow \omega$... finished after one round:

result: win(a), win(b), win(i), all other wins are false. $\Rightarrow H_2$
 \Rightarrow underestimate of true atoms

3rd round: $H_2 = \{\text{the moves}\} \cup \{\text{win}(a), \text{win}(b), \text{win}(i)\}$

as before, now build the reduct P_{H_2} :

first step:

delete from P_{H_2} all rules that contain a negative literal $\neg a$ in the body such that $a \in H_2$,

second step:

delete all remaining negative literals in the bodies of the remaining rules.
(because those are true ... fix them intermediately)

~~win(a) :- move(a,b), not win(b).~~
~~win(a) :- move(a,f), not win(f).~~
~~win(b) :- move(b,c), not win(c).~~
~~win(b) :- move(b,g), not win(g).~~
~~win(b) :- move(b,k), not win(k).~~
~~win(c) :- move(c,d), not win(d).~~
~~win(c) :- move(c,l), not win(l).~~
~~win(d) :- move(d,e), not win(e).~~
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~~win(g) :- move(g,h), not win(h).~~
~~win(g) :- move(g,i), not win(i).~~
~~win(h) :- move(h,m), not win(m).~~
~~win(i) :- move(i,j), not win(j).~~
~~win(l) :- move(l,d), not win(d).~~
~~win(m) :- move(m,h), not win(h).~~

run $T_{PH_2} \rightarrow \omega$... finished after one round:

result: win: a,b,c,d,g,h,i,l,m

... what is missing: not win: e, f, j, k, n

=> overestimate of win, but some (more) are known to be definitively lost